

# [BUSINESS MATHEMATICS]

## मापदण्ड निर्देश (General Instructions)

- परीक्षाती यथासम्भव अपने शब्दों में ही उत्तर दें। (Candidates are required to give their answers in their own words as far as practicable.)
- सभी प्रश्न अनिवार्य हैं। (All questions are compulsory.)

## भाग-अ (Part-A)

**प्र. 1.** यदि  ${}^7P_r = 42$  है, तो  $r$  का मान ज्ञात ए। (If  ${}^7P_r = 42$ , find the value of  $r$ .)

$$\text{Sol. } {}^7P_r = 42$$

$$\Rightarrow \frac{7!}{(7-r)!} = 42$$

$$\Rightarrow \frac{7 \times 6 \times 5!}{(7-r)!} = 7 \times 6$$

$$\Rightarrow 7 \times 6 \times 5! = 7 \times 6 (7-r)!$$

$$\Rightarrow (7-r)! = \frac{7 \times 6 \times 5!}{7 \times 6}$$

$$\Rightarrow (7-r)! = 5!$$

$$\Rightarrow 7-r = 5$$

$$\Rightarrow 7-5 = r$$

$$\therefore r = 2 \quad \text{Ans.}$$

**प्र. 2.** श्रेणी  $1, \sqrt{3}, 3, \dots$  का दसवाँ पद ज्ञात करें।  
(Find the 10th term of the series  $1, \sqrt{3}, 3, \dots$ )

$$\text{Sol. First term, } a = 1$$

$$\text{Common ratio, } r = \frac{\sqrt{3}}{1} = \sqrt{3}$$

$$T_{10} = ?$$

$$T_n = ar^{n-1}$$

$$T_{10} = ar^{10-1}$$

$$= 1(\sqrt{3})^9 = 81\sqrt{3} \quad \text{Ans.}$$

**प्र. 3.** यदि किसी समान्तर श्रेणी का 8वाँ और 25वाँ पद क्रमशः 15 और 49 हैं, तो पहला पद और समान्तर ज्ञात कीजिए। (If 8th and 25th term of an A.P. are 15 and 49 respectively, then find its first term and common difference.)

**Sol.** Let  $a$  = first term and  $d$  = common difference

$$T_8 = 15 \text{ and } T_{25} = 49$$

$$T_8 = a + (8-1)d$$

$$15 = a + 7d \quad \dots(i)$$

$$\text{Also, } T_{25} = a + (25-1)d$$

$$49 = a + 24d \quad \dots(ii)$$

From equation (i) and (ii), we get;

$$a + 7d = 15$$

$$\begin{array}{r} a + 24d = 49 \\ -17d = -34 \\ d = 2 \end{array}$$

Putting the value of  $d = 2$  in equation (i)

$$a + 7 \times 2 = 15$$

$$a = 15 - 14 = 1$$

Hence, first term = 1 and  
common difference = 2. Ans.

**प्र. 4.** यदि  $A = \{11, 12, 13, 14, 15, 16\}$  और  $B = \{11, 12, 15, 16, 17, 18, 19\}$  है, तो  $(A-B)$  और  $(B-A)$  ज्ञात करें। (If  $A = \{11, 12, 13, 14, 15, 16\}$  and  $B = \{11, 12, 15, 16, 17, 18, 19\}$ , find the value of  $(A-B)$  and  $(B-A)$ .)

$$\text{Sol. } A - B = \{11, 12, 13, 14, 15, 16\} - \{11, 12, 15, 16, 17, 18, 19\} = [13, 14, 15]$$

$$B - A = \{11, 12, 15, 16, 17, 18, 19\} - \{11, 12, 13, 14, 15, 16\} = [17, 18, 19] \quad \text{Ans.}$$

**प्र. 5.** 3 व्यक्तियों में 6 पुरस्कारों को फिरने पकार से बौटा जा सकता है, यदि प्रत्येक व्यक्ति को फिरने भी पुरस्कार दिए जा सकते हैं। (In how many ways 6 prizes can be distributed among 3 persons, if each can be given as many prizes?)

**Sol.** Number of persons = 3

Number of prizes = 6

Since each person is eligible for any of the prizes.

So number of ways to distribute the first prize = 3

Similarly number of ways to distribute

the second prize = 3

So that if 6 prize will distribute at there persons

$$= 3 \times 3 \times 3 \times 3 \times 3 \times 3 \\ = 3^6 = 729 \quad \text{Ans.}$$

प्र. 6. मान निकालें (Evaluate :)

$$\begin{vmatrix} 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \end{vmatrix}$$

$$\text{Sol. } \Delta = \begin{vmatrix} 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \end{vmatrix} \\ = 1 \begin{vmatrix} 3 & 9 \\ 4 & 16 \end{vmatrix} - 2 \begin{vmatrix} 1 & 9 \\ 1 & 16 \end{vmatrix} + 4 \begin{vmatrix} 1 & 3 \\ 1 & 4 \end{vmatrix} \\ = 1(48 - 36) - 2(16 - 9) + 4(4 - 3) \\ = 1 \times 12 - 2 \times 7 + 4 \times 1 \\ = 12 - 14 + 4 \\ = 16 - 14 = 2 \quad \text{Ans.}$$

$$\text{प्र. 7. यदि (II) } A = \begin{bmatrix} 3 & 2 & 0 \\ 1 & 0 & 1 \\ 2 & 1 & 3 \end{bmatrix} \text{ हो, तो } A^2 \text{ ज्ञात करें।} \\ (\text{then find } A^2.)$$

$$\text{Sol. } A^2 = A \times A = \begin{bmatrix} 3 & 2 & 0 \\ 1 & 0 & 1 \\ 2 & 1 & 3 \end{bmatrix} \begin{bmatrix} 3 & 2 & 0 \\ 1 & 0 & 1 \\ 2 & 1 & 3 \end{bmatrix} \\ = \begin{bmatrix} 9+2+0 & 6+0+0 & 0+2+0 \\ 3+0+2 & 2+0+1 & 0+0+3 \\ 6+1+6 & 4+0+3 & 0+1+9 \end{bmatrix} \\ = \begin{bmatrix} 11 & 6 & 2 \\ 5 & 3 & 3 \\ 13 & 7 & 10 \end{bmatrix} \quad \text{Ans.}$$

प्र. 8. मान निकालें (Evaluate :)

$$\int \frac{(x^3 + 8)(x-1)}{x^2 - 2x + 4} dx$$

$$\text{Sol. } \int \frac{(x^3 + 8)(x-1)}{x^2 - 2x + 4} dx$$

$$= \int \frac{(x+2)(x^2 - 2x + 4)(x-1)}{(x^2 - 2x + 4)} dx$$

$$= \int (x+2)(x-1) dx$$

$$= \int (x^2 + x - 2) dx$$

$$= \int (x^2 + x - 2) dx$$

$$= \int x^2 dx + \int x dx - \int x^0 dx + C$$

$$= \frac{x^{2+1}}{2+1} + \frac{x^{1+1}}{1+1} - x^{0+1} + C$$

$$= \frac{x^3}{3} + \frac{x^2}{2} - x + C \quad \text{Ans.}$$

प्र. 9. यदि  ${}^n C_5 = {}^n C_7$  है, तो  $n$  का भल ज्ञात करें। (If  ${}^n C_5 = {}^n C_7$ , find the value of  $n$ .)

$$\text{Sol. } {}^n C_5 = {}^n C_7$$

$$\therefore n = 5 + 7 = 12$$

$$\left[ \because {}^n C_p = {}^n C_q \right] \\ \therefore n = p + q \quad \text{Ans.}$$

प्र. 10. एक पाठशाला में 60% विद्यार्थियों ने राष्ट्रीय सुरक्षा कोष में तथा 70% विद्यार्थियों ने राष्ट्रीय बचत योजना में चला दिया। कितने प्रतिशत विद्यार्थियों ने दोनों ही योजनाओं में चला दिया? (In a school 60% students donated in National Security Fund and 70% students donated in National Saving Scheme. How much students donated in both the Schemes?)

**Sol.**  $A = \text{Set of student who donate NSF}$

$B = \text{Set of student who donate NSS}$

Total number of student,  $n(A \cup B) = 100$

$$n(A) = 60, n(B) = 70$$

$$\therefore n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

$$100 = 60 + 70 - n(A \cap B)$$

$$100 = 130 - n(A \cap B)$$

$$n(A \cap B) = 130 - 100 = 30$$

Hence, 30% students donated in both the Scheme. Ans.

प्र. 11. यदि (II)  $y = x^4 + 4x^3 + 5x - 5$  हो, तो (Find)

$$\frac{dy}{dx} \text{ का मान निकालें।}$$

$$\text{Sol. } y = x^4 + 4x^3 + 5x - 5$$

$$\frac{dy}{dx} = \frac{d}{dx}(x^4 + 4x^3 + 5x - 5)$$

$$= \frac{d}{dx}(x^4) + \frac{d}{dx}(4x^3) + \frac{d}{dx}$$

$$(5x) \cdot \frac{d}{dx}(b)$$

$$= 4 \cdot x^{4-1} + 4 \cdot 3x^{3-1} + 5x^{1-1} \cdot 0$$

$$= 4x^3 + 12x^2 + 5 \quad \text{Ans.}$$

प्र. 12. G.P. में तीन संख्याएँ निकालें, जिनकी अनुपर्याप्त 216 तथा योग 21 है। (Find the three numbers in G.P. whose product is 216 and sum is 21.)

**Sol.** Three numbers in G.P. are  $\frac{a}{r}, a$  and  $ar$  respectively.

According to question, product of three numbers is 216.

$$\Rightarrow \frac{a}{r} \times a \times ar = 216$$

$$\Rightarrow a^3 = 216$$

$$\Rightarrow a^3 = 6^3$$

$$\therefore a = 6$$

Also  $\frac{a}{r} + a + ar = 21$

$$\Rightarrow \frac{a + ar + ar^2}{r} = 21$$

$$\Rightarrow a + ar + ar^2 = 21r$$

$$\Rightarrow a + ar + ar^2 - 21r = 0$$

(putting the value of  $a = 6$ )

$$\Rightarrow 6 + 6r + 6r^2 - 21r = 0$$

$$\Rightarrow 6r^2 - 21r + 6r + 6 = 0$$

$$\Rightarrow 3(2r^2 - 5r + 2) = 0$$

$$\Rightarrow 2r^2 - r - 4r + 2 = 0$$

$$\Rightarrow 2r^2 - 4 - 4r + 2 = 0$$

$$\Rightarrow 2r(2r - 1) - 2(2r - 1) = 0$$

$$(r - 2)(2r - 1) = 0$$

If  $r - 2 = 0$  and  $2r - 1 = 0$

$$\Rightarrow r = 2$$

and  $2r = 1 \therefore r = \frac{1}{2}$

When  $r^2 = \frac{1}{2}$ , then numbers are  $\frac{6}{2},$

6, 6  $\times$  2 i.e., 3, 6, 12.

**प्र. 13.** प्रमाणित करें। (Prove that)

$$\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix} = (a+b+c)^3$$

**Sol.**  $\begin{vmatrix} a-b-c & 2a & 2a \\ 2b & b-c-a & 2b \\ 2c & 2c & c-a-b \end{vmatrix}$

Operating  $c_1 \rightarrow c_1 - c_2$   
and  $c_2 \rightarrow c_2 - c_3$

$$= \begin{vmatrix} -(a+b+c) & 0 & 2a \\ a+b+c & -(a+b+c) & 2b \\ 0 & a+b+c & c-a-b \end{vmatrix}$$

$$= (a+b+c)(a+b+c) \begin{vmatrix} -1 & 0 & 2a \\ 1 & -1 & 2b \\ 0 & 1 & c-a-b \end{vmatrix}$$

$$r_2 \rightarrow r_2 + r_1$$

$$= (a+b+c)^2 \begin{vmatrix} -1 & 0 & 2a \\ 0 & -1 & 2b+2a \\ 0 & 1 & c-a-b \end{vmatrix}$$

$$= (a+b+c)^2(-1) \begin{vmatrix} -1 & 2b+2a \\ 1 & c-a-b \end{vmatrix}$$

$$= (a+b+c)^2(-1)(-c+a+b-2b-2a)$$

$$= (a+b+c)^2(-1) \times (-c-a-b)$$

$$= (a+b+c)^2.(a+b+c)$$

$$= (a+b+c)^3 \quad \text{Proved.}$$

**प्र. 14.** एक थैले में 3 लाली, 5 काली, 5 पीली गेंद हैं। एक गेंद निकालने पर उसके लाल या पीली गेंद निकालने की प्रायिकता है ? (A bag contains 3 red, 5 black, and 5 yellow balls. What is the probability of getting red or yellow in a single draw of one?)

**Sol.** Total balls  $[n(S)] = 3 + 5 + 5 = 13$

Let, A = Event of getting a red ball

B = Event of getting a yellow ball

Probability of getting red ball, [P(A)]

$$= \frac{n(A)}{n(S)} = \frac{3}{13}$$

Probability of getting yellow ball, [P(B)]

$$= \frac{n(B)}{n(S)} = \frac{5}{13}$$

$\therefore$  Required probability = P(A) + P(B)

$$= \frac{3}{13} + \frac{5}{13} = \frac{8}{13} \quad \text{Ans.}$$

**प्र. 15.** हरात्मक माध्य क्या है ? इसका समीकरण सूत्र दीजिये। (What is Harmonic Mean ? Give the equation.)

**Ans.** विभिन्न चरों का हरात्मक माध्य उसके मूल्यों के व्युत्कर्षों के समान्तर माध्य का व्युत्कर्ष होता है प्रति रूपया के रूप में दिए गए मूल्य आदि को औसत मात्रा का पता करने के लिए विशेष रूप से प्रयोग में लाई जाती है। (Harmonic mean is the reciprocal of the arithmetic mean of the reciprocal of all the items of a group.)

Formula :

$$\text{H.M.} = \frac{N}{\frac{1}{x_1} + \frac{1}{x_2} + \frac{1}{x_3} + \dots + \frac{1}{x_n}}$$



$$\therefore \text{Mode Class} = 39.5 - 49.5 \\ I_1 = 39.5, i = 10, f_1 = 36, f_0 = 29, f_2 = 25$$

$$\text{Mode } (Z) = I_1 + \left( \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times i \\ = 39.5 + \left( \frac{36 - 29}{2 \cdot 36 - 29 - 25} \right) \times 10 \\ = 39.5 + \frac{7}{18} \times 10 = 39.5 + \frac{35}{9} \\ = 39.5 + 3.88 = 43.38 \quad \text{Ans.}$$

Q. 20. विभिन्न वर्षों के लिए किसी जिले के जनसंख्या जिस है 2005 के लिए जनसंख्या जात करें। (The population of different Districts for different years are as follows. Find the population 2015.)

वर्ष (Year)	2000	2001	2002	2003	2004
जनसंख्या (लाखों में) [Population (in million)]	7	9	36	14	16

Sol.	Year	Population (in million)
	2000	7
	2001	9
	2002	?
	2003	14
	2004	16
	2005	?

$$\therefore (y - 1)^4 = 0$$

$$y_4 - 4y_3 + 6y_2 - 4y_1 + y_0 = 0$$

$$16 - 4 \times 14 + 6y_2 - 4 \times 9 + 7 = 0$$

$$16 - 56 + 6y_2 - 36 + 7 = 0$$

$$16 - 7 - 56 - 36 + 6y_2 = 0$$

$$23 - 92 + 6y_2 = 0$$

$$6y_2 = 92 - 23$$

$$6y_2 = 69 \therefore y_2 = \frac{69}{6} = 11.5$$

Population of 2005,

$$(y - 1)^5 = 0$$

$$y_5 - 5y_4 + 10y_3 - 10y_2 + 5y_1 - y_0 = 0$$

$$y_5 - 5 \times 16 + 10 \times 14 - 10 \times 9 + 5 \times 7 = 0$$

$$y_5 - 80 + 140 - 115 + 45 - 7 = 0$$

$$y_5 + 140 + 45 - 80 - 115 + 7 = 0$$

$$y_5 + 185 - 202 = 0$$

$$y_5 = 202 - 185$$

$$y_5 = 17 \text{ million} \quad \text{Ans.}$$

प्र. 21. निम्नलिखित गारमी के गढ़वाल फॉलोवर्स  
(Calculate mode from the following data )

आकार (Size)	0-5	5-10	10-15	15-20	20-25	25-30
आवृत्ति (Frequency)	10	25	50	7	13	5

Sol.	C.I.	f
	0-5	10
	5-10	25 $f_0$
	10-15	50 $f_1$
	15-20	7 $f_2$
	20-25	13
	25-30	5

By inspection method:

$$\text{Highest Frequency} = 50$$

$$\therefore \text{Mode Class} = 10 - 15$$

$$I_1 = 10, i = 5, f_1 = 50, f_0 = 25, f_2 = 7$$

$$Z = I_1 + \left( \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times i$$

$$= 10 + \left( \frac{50 - 25}{2 \cdot 50 - 25 - 7} \right) \times 5$$

$$= 10 + \left( \frac{25}{100 - 32} \right) \times 5$$

$$= 10 + 1.84 = 11.84 \quad \text{Ans.}$$

प्र. 22. एक व्यक्ति 4 में से 3 निश्चये मर्दी लगाता है और दूसरा व्यक्ति 3 में से 2 निश्चये मर्दी लगाता है। यदि दोनों ही व्यक्ति एक गाथ इटते हैं, तो लक्ष्य के भेटने की संभायना हात कीजिए। (A person is known to hit the target 3 out of 4 shots whereas another person is known to hit the target 2 out of 3 shots. Find the probability of the target being hit at all when they both try ?)

Sol. The probability that first person hit the target,  $P(A) = \frac{3}{4}$

Probability that the second person hits the target,  $P(B) = \frac{2}{3}$

The events are not mutually exclusive since both of them may hit the target

The probability that both may hit the target

$$P(A \cup B) = \frac{3}{4} + \frac{2}{3}$$

$$\therefore P(A \text{ or } B) = P(A) + P(B) - P(A \cap B)$$

$$= \left( \frac{3}{4} + \frac{2}{3} \right) - \left( \frac{3}{4} \times \frac{2}{3} \right) = \frac{9+8}{12} - \frac{6}{12}$$

$$= \frac{17-6}{12} = \frac{11}{12}$$

Ans.

Q. 23. किसी नियुक्त ग्रन्डी से व्यवस्था वाले फिल्म द्वारा बोली गई आमत्र वर्षों (Find the trend line by the least square method from the following data.)

Sol.

Year	Time Deviation from 2002 ( $x$ )	$x^2$	Price $y$	$xy$	Trend $y_c = a + bx$
2000	-5	25	107	-535	102.73
2001	-3	9	110	-330	110
2002	-1	1	114	-114	111.22
2003	1	1	112	112	112.44
2004	3	9	115	345	113.66
2005	5	25	113	565	114.88
$N = 6$		$\sum x^2 = 70$	$\sum y = 671$	$\sum xy = 43$	$\sum y_c = 670.93 \text{ or } 671$

$$a = \frac{\sum y}{N} = \frac{671}{6} = 111.83 \text{ and}$$

$$b = \frac{\sum xy}{\sum x^2} = \frac{43}{70} = 0.61$$

$\Rightarrow$  Calculation of Trend value of the following year :

$$y_c = a + bx$$

$$\begin{aligned} \text{Year 2000} &= 111.83 + 0.61(-5) \\ &= 111.83 - 3.05 = 108.78 \end{aligned}$$

$$\begin{aligned} \text{Year 2001} &= 111.83 + 0.61(-3) \\ &= 111.83 - 1.83 = 110 \end{aligned}$$

$$\begin{aligned} \text{Year 2002} &= 111.83 + 0.61(-1) \\ &= 111.83 - 0.61 = 111.22 \end{aligned}$$

$$\begin{aligned} \text{Year 2003} &= 111.83 + 0.61(1) \\ &= 111.83 + 0.61 = 112.44 \end{aligned}$$

$$\begin{aligned} \text{Year 2004} &= 111.83 + 0.61(3) \\ &= 111.83 + 1.83 = 113.66 \end{aligned}$$

$$\begin{aligned} \text{Year 2005} &= 111.83 + 0.61(5) \\ &= 111.83 + 3.05 \\ &= 114.88 \quad \text{Ans.} \end{aligned}$$

Q. 24. दो पांसे घेके लाले हैं। राधाकाना द्वारा योगिता कि दोनों न लंबे 7 और लंबे 11। (If a pair of dice

is thrown, find the probability that the sum is neither 7 nor 11.)

Sol. Let, A = Event of getting a sum of 7

B = Event of getting a sum of 11

Expected outcomes are  $6 \times 6$

$$= n(S) = 36$$

$$A = \{(1, 6), (6, 1), (5, 2), (2, 5), (3, 4), (4, 3)\}$$

$$n(A) = 6$$

Probability of getting A,

$$P(P(A)) = \frac{n(A)}{n(S)} = \frac{6}{36} = \frac{1}{6}$$

$$B = \{(6, 5), (5, 6)\}$$

$$n(B) = 2$$

Probability of getting P(P(B))

$$= \frac{n(B)}{n(S)} = \frac{2}{36} = \frac{1}{18}$$

The probability that the sum is neither 7 and 11

$$= 1 - [P(A) + P(B)] = 1 - \left[ \frac{1}{6} + \frac{1}{18} \right]$$

$$= 1 - \left[ \frac{3+1}{18} \right] = 1 - \frac{4}{18} = \frac{14}{18} = \frac{7}{9}$$

$$\therefore \text{Required Probability} = \frac{7}{9}$$

**Ans.**

- प्र. 25. निम्न आँकड़ों से अज्ञात आवृत्ति की गणना करें,  
यदि माध्य 67.45 हो। (Find the missing frequency from the following data, if Mean is 67.45.)

आकार (Size)	60-62	63-65	66-68	69-71	72-74
आवृत्ति (Frequency)	15	51	?	81	24
S. S.					

Ans.  
गलै।

C.I.	m.v.(x)	f	fx
60 - 62	61	15	915
63 - 65	64	54	3456
66 - 68	67	$f_1$	$67f_1$
69 - 71	70	81	5670
72 - 74	73	24	1752
		$\Sigma f = 174$ $+ f_1$	$\Sigma fx = 11,793$ $+ 67f_1$

### Direct Method

$$\text{Mean } (\bar{x}) = \frac{\sum fx}{\sum f}$$

$$67.45 = \frac{11793 + 67f_1}{174 + f_1}$$

$$67.45(174 + f_1) = 11793 + 67f_1$$

$$11736.3 + 67.45f_1 = 11793 + 67f_1$$

$$67.45f_1 - 67f_1 = 11793 - 11736.3$$

$$0.45f_1 = 56.7$$

$$f_1 = \frac{56.7}{0.45}$$

$$f_1 = 126$$

Ans.